Dynamic 3D Modelling of the Human Left Ventricle

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Abstract—Visualization and quantification of cardiac function is important in diagnosing and management of heart diseases. As quantitative analysis performed on the images is crucial to understand the heart mechanics, an accurate diagnosis of heart conditions can be done if clear visualization of ventricular volume, mass and function are obtained from echo-cardiograph images. This paper presents a technique to develop a dynamic three dimensional model of the left ventricle of the human heart to illustrate both the shape and motion of the ventricle along a cardiac cycle. The proposed methodology includes a multistage approach that involves a pipeline of image processing routines such as filtering, contrast stretching and binary morphology to isolate heart tissues. Subsequently, cubic spline curves are used to generate a smooth surface of the heart muscle using a set of control points extracted from the locations of boundaries of the heart muscle. A complete pulse included 40 images and it takes an average of 16.0665 seconds for the model to deform over a pulse.

Keywords—left ventricle, echocardiography, dynamic modelling

I. INTRODUCTION

Visualization and quantification of cardiac function is important in diagnosing and managing heart diseases. In recent times, heart failure has caused high morbidity and mortality rates in humans with the incidence and prevalence are increasing due to the use of alcohol, physical inactivity, an unhealthy diet [9].

With current diagnosing techniques such as echocardiography, cardiac MRI and CT, it is possible to obtain clear grey scale images in 2D with patient data [10]. These images can be used to extract cardiac information of the patient using computer assisted tools. Noninvasive techniques are much popular and acceptable for the study of the human heart in vivo. Present noninvasive diagnosing techniques, as mentioned earlier, provide only a 2D view of the organ taken at a particular instance of time. Some of these images are quite confounded by external factors making it difficult to visualize the actual anatomy of the heart. Hence, it requires analyzing a series of images taken at different views at different times to arrive at clinically accurate conclusions. Such an analysis is a manual process that consumes time and requires expertise knowledge. Moreover, these images can provide only a qualitative analysis at the hands of a medical practitioner.

A quantitative analysis performed on the images is crucial to understand the mechanics of the heart. This gives us a framework to investigate the shape and motion of the heart throughout a cardiac cycle by giving important parameters of study like strain and strain rate of myocardium.

Pathological investigations of heart diseases are mainly concerned on the left ventricle (LV) of the heart because the consequence of a heart disease is better visualized by the left ventricle. Left ventricular hypertrophy is one such instance where the myocardium of the left ventricle gradually becomes thick and loses its ability to relax due to a cardiovascular disease [11].

Biomechanics is the field of study that analyses mechanical properties of biological systems and how the structure of a system deforms when subjected to certain forces. These models are now becoming popular in clinical practice as a tool in surgical planning because of their ability to display deformations on soft tissues in real time. Such therapeutic simulations can be tried out with the model before the actual surgery [1].

The main objective of the work presented in this paper is to digitally reconstruct the shape and motion of the left ventricle of the heart by a three dimensional deformable model using a series of image processing routines.

II. RECENT WORK

Santos et. al. [2] have used spatial linear space domain filter with a 3x3 neighborhood to remove noise from echocardiograph images and then a histogram modification is used to enhance endocardial and epicardial boundaries of the left ventricle. The histogram modification is manipulated by background subtraction and linear contrast stretching. Median filter is also discussed as an effective noise filtering technique for echo-cardiographs.

A morphological filtering technique to remove noise in the ventricle cavity in echocardiograph images is presented in [3]. Although the method performs well in removing noise in the cavity, the resulting image exhibits discontinuities at the edges.

In [4] and [5], multistage hybrid segmentation methods which combine morphological reconstruction and fast marching algorithms are proposed to segment dynamic CT images of the beating heart. Quantitative evaluation on 50 canine CT images against ground truth had demonstrated a similarity index of 0.956.
A multimodality segmentation algorithm to segment the LV from cardiac images based on deformable models is presented in [6]. Four parameters govern forces on the model and satisfy an Euler-Lagrange equation at the equilibrium. Further, it gives a methodology to incorporate temporal information to the edge detection to filter out spurious edges.

III. PROPOSED METHODOLOGY

The proposed methodology includes a multistage approach where a series of raw echo images is taken and cropped into a fixed size such that they all significantly represent the LV region of interest (ROI). Then, the fiducial marks present in these images are removed as they might affect post-processing tasks. Median filtering [7] is applied to reduce speckle noise (Fig. 1(b) and 1(e)) and subsequently, a linear contrast stretch is applied to enhance a selected intensity range highlighting the difference between the myocardium and the blood pool (Fig. 1(e) and 1(f)).

The above pre-processed images are taken as the input to the segmentation process which is also a multistage procedure as seen in Fig. 2. First, binary images are obtained by a global thresholding scheme applied for all the short axis images whereas an adaptive thresholding (window size 130 and threshold 0.01) is applied for long axis images. The resulting image is then recursively eroded using a disk shaped structuring element until the LV cavity is completely separated from its connected regions. It is followed by labelling the connected components to label maximally connected regions of foreground pixels in the resulted binary image. Then, using a priori knowledge, the LV is extracted by considering the average size of a human LV. The extracted LV is then recursively dilated with the same structuring element to recover lost pixels during the previous erosion. It is possible that some speckle noise may have been left out during the pre-processing stage. As such, morphological filling is applied at the next stage.

The segmented image is taken as the input to the boundary point extraction process. As the first step, the boundary of the LV is extracted by applying the Sobel filter. Then, a radial search is performed by rotating the image around its central axis and taking the boundary point at each 10° degree. The segmented image series obtained at $t = t_0$ is used to reconstruct the initial LV geometry in the 3D space. The model is defined in spheroidal coordinate system ($\lambda$, $\mu$, $\theta$) and the proposed steps are as follows:

First, the following are calculated in order to simplyfy the task.

- Centroid coordinates of the LV in every short-axis image slice: ($x_c$, $y_c$)
- Location of the base in a long-axis image slice: ($x_b$, $y_b$)
- Location of the apex in a long-axis image slice: ($x_a$, $y_a$)

![Figure 1: Pre-processing step (short axis-base): (a) & (d) Original images, (b) & (e) median filtering, (c) & (f) contrast stretching.](image1)

![Figure 2: Output images of segmentation steps (short axis-apex): (a) pre-processing, (b) global thresholding, (c) boundary correction, (d) inverse binary image, (e) erosion, (f) connected component labelling, (g) extracted LV, (h) dilation and (i) morphological filling.](image2)

At first, the long axis image slices are used to obtain the distance from the apex to the base. This distance is used as an overall scale factor for a voxel. Subsequently, the segmented short-axis slices are transformed into 3D space using the transformation equation.

$$v_i = T_e R T_d v_0$$

where $v_0 = (x_0, y_0, z_0)^T$ represent the homogeneous coordinates of a point in the 3D plane and $v_1 = (x_1, y_1, z_1)^T$ represents its transformed coordinate position as a 3D voxel. $T_e$, $T_d$ and $R$ represent translation and rotation matrices, respectively.

The images are placed in the 3D space by first translating them into the origin of the xyz coordinate system and rotated according to the angle in which they are acquired by the probe. Subsequently, the images are again translated along the z axis such that the base short axis plane is located at distance $d$ from the origin, mid ventricular plane at $2d/3$ distance and apex plane located at $d/5$ distance as in Fig. 3.
Although the segmented slices are placed at its correct position in the voxel, a continuous volume cannot be obtained until discrete locations of control points are known. Hence, the volume is re-sampled and reconstructed in 3D by a finite number of points sufficient to represent the LV shape. A straight line is rotated around the z axis and at every 10\(^\text{th}\) degree and a control point is taken at the intersecting point with the short-axis image.

Reconstruction of the initial geometry is done using cubic spline curves with Lagrange end conditions. After constructing the wireframe, Gouraud lighting model is applied to obtain a smooth shading.

Considering that every image plane is spatially fixed during a heart beat, some of the structures move in or out from the plane. However, such through-plane motion cannot be captured from data points on the image plane.

Figure 5 shows the location of image data points at two different time intervals \(t_1\) and \(t_2\). Initially, at \(t_1\), the image data point coincides with the material point. However, the motion of the image data point between these two time intervals approximates to the components on the image plane.

However, the motion of the material point can be captured from images at two perpendicular directions taken at \(t_2\). From the slice of a short axis image, we can extract the \(x, y\) components which contain the in-plane motion. Further, from the long axis image, we can extract the \(z\)-component containing the through-plane motion.

Figure 6: Outputs of LV height extraction from long axis images. (a) segmented long axis LV, (b) boundary extracted, (c) maximum and minimum points and (d) estimated height.
Before constructing a method to deform the initial geometry the continuous material domain \((u,v)\) is tessellated into a mesh of M elements. We approximate \(x\) as the weighted sum of piecewise polynomial functions \(N^i\) such that

\[
x(u, v, t) = \sum_{i=0}^{n} N^i(u, v)q^i(t)
\]

where \(q^i\) is a vector of the nodal variables associated with the mesh node \(i\). The model is deformed according to the following equation

\[
q^{t+1} = q^t + TDx, y, z, J
\]

where \(T\) is a transformation matrix concerning translation and \(D\) the displacement field calculated

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REFERENCES


